# **Package 'quartets'**

April 14, 2023

Type Package

Title Datasets to Help Teach Statistics

Version 0.1.1

Description In the spirit of Anscombe's quartet, this package includes datasets that demonstrate the importance of visualizing your data, the importance of not relying on statistical summary measures alone, and why additional assumptions about the data generating mechanism are needed when estimating causal effects. The package includes ``Anscombe's Quar-tet" (Anscombe 1973) <doi:10.1080/00031305.1973.10478966>, D'Agostino McGowan & Barrett (2023) ``Causal Quartet" <doi:10.48550/arXiv.2304.02683>, ``Datasaurus Dozen" (Matejka & Fitzmaurice 2017), ``Interaction Triptych" (Rohrer & Arslan 2021) <doi:10.1177/25152459211007368>, ``Rashomon Quartet" (Biecek et al. 2023) <doi:10.48550/arXiv.2302.13356>, and Gelman ``Variation and Heterogeneity Causal Quartets" (Gelman et al. 2023) <doi:10.48550/arXiv.2302.12878>.

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https://r-causal.github.io/quartets/

BugReports https://github.com/r-causal/quartets/issues

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anscombe\_leverage Anscombe's Quartet High Leverage Data

# Description

This dataset contains 11 observations generated by Francis Anscombe to demonstrate that statistical summary measures alone cannot capture the full relationship between two variables (here, x and y). Anscombe emphasized the importance of visualizing data prior to calculating summary statistics.

# Usage

anscombe\_leverage

# Format

A dataframe with 11 rows and 2 variables:

- x: the x-variable
- y: the y-variable

#### Details

This Dataset has a no relationship between x and y with a single high leverage point Additionally, the following statistical summaries hold:

- mean of x: 9
- variance of x: 11

#### anscombe\_linear

- mean of y: 7.5
- variance of y: 4.125
- correlation between x and y: 0.816
- linear regression between x and y: y = 3 + 0.5x
- $R^2$  for the regression: 0.67

# References

Anscombe, F. J. (1973). "Graphs in Statistical Analysis". American Statistician. 27 (1): 17–21. doi:10.1080/00031305.1973.10478966. JSTOR 2682899.

anscombe\_linear Anscombe's Quartet Linear Data

# Description

This dataset contains 11 observations generated by Francis Anscombe to demonstrate that statistical summary measures alone cannot capture the full relationship between two variables (here, x and y). Anscombe emphasized the importance of visualizing data prior to calculating summary statistics.

# Usage

anscombe\_linear

# Format

A dataframe with 11 rows and 2 variables:

- x: the x-variable
- y: the y-variable

#### Details

This Dataset has a linear relationship between x and y Additionally, the following statistical summaries hold:

- mean of x: 9
- variance of x: 11
- mean of y: 7.5
- variance of y: 4.125
- correlation between x and y: 0.816
- linear regression between x and y: y = 3 + 0.5x
- $R^2$  for the regression: 0.67

#### References

anscombe\_nonlinear Anscombe's Quartet Nonlinear Data

# Description

This dataset contains 11 observations generated by Francis Anscombe to demonstrate that statistical summary measures alone cannot capture the full relationship between two variables (here, x and y). Anscombe emphasized the importance of visualizing data prior to calculating summary statistics.

#### Usage

anscombe\_nonlinear

# Format

A dataframe with 11 rows and 2 variables:

- x: the x-variable
- y: the y-variable

# Details

This Dataset has a nonlinear relationship between x and y

Additionally, the following statistical summaries hold:

- mean of x: 9
- variance of x: 11
- mean of y: 7.5
- variance of y: 4.125
- correlation between x and y: 0.816
- linear regression between x and y: y = 3 + 0.5x
- $R^2$  for the regression: 0.67

# References

This dataset contains 11 observations generated by Francis Anscombe to demonstrate that statistical summary measures alone cannot capture the full relationship between two variables (here, x and y). Anscombe emphasized the importance of visualizing data prior to calculating summary statistics.

#### Usage

anscombe\_outlier

# Format

A dataframe with 11 rows and 2 variables:

- x: the x-variable
- y: the y-variable

# Details

This Dataset has a linear relationship between x and y with a single outlier

Additionally, the following statistical summaries hold:

- mean of x: 9
- variance of x: 11
- mean of y: 7.5
- variance of y: 4.125
- correlation between x and y: 0.816
- linear regression between x and y: y = 3 + 0.5x
- $R^2$  for the regression: 0.67

# References

anscombe\_quartet

# Description

This dataset contains 44 observations, 11 observations from 4 datasets generated by Francis Anscombe to demonstrate that statistical summary measures alone cannot capture the full relationship between two variables (here, x and y). Anscombe emphasized the importance of visualizing data prior to calculating summary statistics.

#### Usage

anscombe\_quartet

#### Format

A dataframe with 44 rows and 3 variables:

- dataset: the dataset the values come from
- x: the x-variable
- y: the y-variable

# Details

- Dataset 1 has a linear relationship between x and y
- Dataset 2 has shows a nonlinear relationship between x and y
- Dataset 3 has a linear relationship between x and y with a single outlier
- Dataset 4 has shows no relationship between x and y with a single outlier that serves as a high-leverage point.

In each of the datasets the following statistical summaries hold:

- mean of x: 9
- variance of x: 11
- mean of y: 7.5
- variance of y: 4.125
- correlation between x and y: 0.816
- linear regression between x and y: y = 3 + 0.5x
- $R^2$  for the regression: 0.67

# References

This dataset contains 100 observations, generated under the following mechanism:  $X \sim N(0, 1)$  (exposure)  $Y \sim X + N(0,1)$  (outcome)  $Z \sim 0.45X + 0.77Y + N(0, 1)$  (measured factor: collider)

#### Usage

causal\_collider

# Format

A dataframe with 100 rows and 3 variables:

- exposure: exposure
- outcome: outcome
- covariate: a known factor (collider)

# References

D'Agostino McGowan L, Barrett M (2023). Causal inference is not a statistical problem. Preprint arXiv:2304.02683v1.

causal\_collider\_time Time-varying Causal Quartet Data

# Description

These datasets contains 100 observations, each generated under a different data generating mechanism:

- (1) A collider
- (2) A confounder
- (3) A mediator
- (4) M-bias

#### Usage

causal\_collider\_time

causal\_confounding\_time

causal\_mediator\_time

causal\_m\_bias\_time

causal\_quartet\_time

# Format

causal\_collider\_time: A dataframe with 100 rows and 7 variables:

- covariate\_baseline: known factor measured at baseline
- exposure\_baseline: exposure measured at baseline
- outcome\_baseline: outcome measured at baseline
- exposure\_followup: exposure measured at the followup visit (final time)
- outcome\_followup: outcome measured at the followup visit (final time)
- covariate\_followup: known factor measured at the followup visit (final time)

causal\_confounding\_time: A dataframe with 100 rows and 7 variables:

- covariate\_baseline: known factor measured at baseline
- exposure\_baseline: exposure measured at baseline
- outcome\_baseline: outcome measured at baseline
- exposure\_followup: exposure measured at the followup visit (final time)
- outcome\_followup: outcome measured at the followup visit (final time)
- covariate\_followup: known factor measured at the followup visit (final time)

causal\_mediator\_time: A dataframe with 100 rows and 7 variables:

- covariate\_baseline: known factor measured at baseline
- exposure\_baseline: exposure measured at baseline
- outcome\_baseline: outcome measured at baseline
- covariate\_mid: known factor measured at some mid-point
- exposure\_mid: exposure measured at some mid-point
- outcome\_mid: outcome measured at some mid-point
- exposure\_followup: exposure measured at the followup visit (final time)
- outcome\_followup: outcome measured at the followup visit (final time)
- covariate\_followup: known factor measured at the followup visit (final time)

causal\_m\_bias\_time: A dataframe with 100 rows and 9 variables:

- u1: unmeasured factor
- u2: unmeasured factor
- covariate\_baseline: known factor measured at baseline
- exposure\_baseline: exposure measured at baseline
- outcome\_baseline: outcome measured at baseline
- exposure\_followup: exposure measured at the followup visit (final time)
- outcome\_followup: outcome measured at the followup visit (final time)
- covariate\_followup: known factor measured at the followup visit (final time)

An object of class tbl\_df (inherits from tbl, data.frame) with 400 rows and 12 columns.

#### Details

There are two time points:

- baseline
- · follow up

These datasets help demonstrate that a model that includes only pre-exposure covariates (that is, only adjusting for covariates measured at baseline), will be less prone to potential biases. Adjusting for only pre-exposure covariates "solves" the bias in datasets 1-3. It does not solve the data generated under the "M-bias" scenario, however this is more of a toy example, it has been shown many times that the assumptions needed for this M-bias to hold are often not ones we practically see in data analysis.

# References

D'Agostino McGowan L, Barrett M (2023). Causal inference is not a statistical problem. Preprint arXiv:2304.02683v1.

# Examples

```
## incorrect model because covariate is post-treatment
lm(outcome_followup ~ exposure_baseline + covariate_followup,
    data = causal_collider_time)
## correct model because covariate is pre-treatment
## even though the true mechanism dictates that the covariate is a collider,
## because the pre-exposure variable is used, the collider bias does not
## occur.
lm(outcome_followup ~ exposure_baseline + covariate_baseline,
    data = causal_collider_time)
```

causal\_confounding Confounder Data

#### Description

This dataset contains 100 observations, generated under the following mechanism:  $Z \sim N(0, 1)$  (measured factor: confounder)  $X \sim Z + N(0,1)$  (exposure)  $Y \sim 0.5X + Z + N(0, 1)$  (outcome)

#### Usage

causal\_confounding

#### Format

A dataframe with 100 rows and 3:

- covariate: a known factor (confounder)
- exposure: exposure
- outcome: outcome

#### References

D'Agostino McGowan L, Barrett M (2023). Causal inference is not a statistical problem. Preprint arXiv:2304.02683v1.

causal\_mediator Mediator Data

# Description

This dataset contains 100 observations, generated under the following mechanism:  $X \sim N(0, 1)$  (exposure)  $Z \sim X + N(0,1)$  (measured factor: mediator)  $Y \sim Z + N(0, 1)$  (outcome)

# Usage

causal\_mediator

## Format

A dataframe with 100 rows and 3 variables:

- exposure: exposure
- covariate: a known factor (mediator)
- outcome: outcome

#### causal\_m\_bias

#### References

D'Agostino McGowan L, Barrett M (2023). Causal inference is not a statistical problem. Preprint arXiv:2304.02683v1.

causal\_m\_bias M-Bias Data

# Description

This dataset contains 100 observations, generated under the following mechanism: U1 ~ N(0, 1) U2 ~ N(0, 1) Z ~ 8 U1 + U2 + N(0, 1) (measured factor) X ~ U1 + N(0, 1) (exposure) Y ~ X + U2 + N(0, 1) (outcome)

# Usage

causal\_m\_bias

# Format

A dataframe with 100 rows and 5 variables:

- u1: an unknown factor
- u2: an unknown factor
- covariate: a known factor
- exposure: exposure
- outcome: outcome

# References

D'Agostino McGowan L, Barrett M (2023). Causal inference is not a statistical problem. Preprint arXiv:2304.02683v1.

causal\_quartet Causal Quartet Data

# Description

This dataset contains 400 observations, each generated under a different data generating mechanism:

- (1) A collider
- (2) A confounder
- (3) A mediator
- (4) M-bias

#### Usage

causal\_quartet

#### Format

A dataframe with 400 rows and 6 variables:

- dataset: The data generating mechanism
- exposure: exposure
- outcome: outcome
- covariate: a known factor
- u1: an unknown factor
- u2: an unknown factor

# References

D'Agostino McGowan L, Barrett M (2023). Causal inference is not a statistical problem. Preprint arXiv:2304.02683v1.

datasaurus\_dozen Datasaurus Dozen Data

#### Description

A dataset containing 12 datasets that are equal in mean, variance, and Pearson's correlation but very different when visualized.

# Usage

datasaurus\_dozen

# Format

A data frame with 1846 rows and 3 variables:

- dataset: the dataset the values come from
- x: the x-variable
- y: the y-variable

#### References

Davies R, Locke S, D'Agostino McGowan L (2022). *datasauRus: Datasets from the Datasaurus Dozen*. R package version 0.1.6, https://CRAN.R-project.org/package=datasauRus.

Matejka, J., & Fitzmaurice, G. (2017). Same Stats, Different Graphs: Generating Datasets with Varied Appearance and Identical Statistics through Simulated Annealing. CHI 2017 Conference proceedings: ACM SIGCHI Conference on Human Factors in Computing Systems. Retrieved from https://www.autodesk.com/research/publications/same-stats-different-graphs

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heterogeneous\_causal\_quartet

Gelman Heterogeneity Causal Quartet Data

# Description

This dataset contains 88 observations, each generated under a different mechanism treatment heterogeneity with respect to some pre-exposure characteristic, z:

- (1) Linear interaction
- (2) No effect then steady increase
- (3) Plateau
- (4) Intermediate zone with large effects

# Usage

heterogeneous\_causal\_quartet

#### Format

A dataframe with 88 rows and 5 variables:

- dataset: The data generating mechanism
- exposure: exposure
- covariate: a pre-exposure factor
- outcome: outcome
- .causal\_effect: latent true causal effect

# References

Gelman, A., Hullman, J., & Kennedy, L. (2023). Causal quartets: Different ways to attain the same average treatment effect. arXiv preprint arXiv:2302.12878.

Hullman J (2023). causalQuartet: Create Causal Quartets for Interrogating Average Treatment Effects. R package version 0.0.0.9000.

This dataset contains 2,700 observations, generated under 3 different conditions

- (1) Ideal case
- (2) Floor effect, No latent interaction
- (3) Smaller correlation at larger slope

#### Usage

interaction\_triptych

# Format

A dataframe with 2700 rows and 5 variables:

- dataset: ideal, floor, or smaller correlation at larger slope
- moderator: a factor that potentially interacts with x, values: low, medium, or high
- x
- y

#### Details

In the ideal scenario, only the slopes differ by moderator level. In the "floor effect" scenario, there is an illusion of an interaction, even though only main effects were simulated. In the third scenario, the slopes increase with higher moderator values but the correlation decreases. Running only a linear model would not allow for appropriate differentiation between these effects.

In each case there is a potential moderator with "low" "medium" and "high" values.

# References

Rohrer, Julia M., and Ruben C. Arslan. "Precise answers to vague questions: Issues with interactions." Advances in Methods and Practices in Psychological Science 4.2 (2021): 25152459211007368.

This dataset contains 2,000 observations, 1,000 training observations and 1,000 testing observations. These were generated such that 4 modeling techniques (regression tree, linear model, neural network, random forest) will yield the same  $R^2$  and RMSE but will fit the models very differently.

# Usage

rashomon\_quartet
rashomon\_quartet\_train

 $rashomon\_quartet\_test$ 

# Format

rashomon\_quartet: A dataframe with 2000 rows and 5 variables:

- split: train, test
- x1
- x2
- x3
- y

rashomon\_quartet\_train: A dataframe with 1000 rows and 4 variables:

- x1
- x2
- x3
- y

rashomon\_quartet\_test: A dataframe with 1000 rows and 4 variables:

- x1
- x2
- x3
- y

#### Details

There are three explanatory variables x1, x2, x3 and one outcome y generated as:

 $y = \sin((3x_1 + x_2)/5) + \varepsilon$ 

where  $\varepsilon \sim N(0, 1/3)$  and  $[x_1, x_2, x_3] \sim N(0, \Sigma_{3x3})$  and  $\Sigma_{3x3}$  has 1 on the diagonal and 0.9 elsewhere.

If fit using the following hyperparameters, each model will yield an  $R^2$  of 0.73 and an RMSE of 0.354

- Regression tree: max depth: 3, min split: 250
- · Linear model: all main effects
- Random Forest: mtry: 1, number of trees: 100
- Neural network: hidden neurons in each layer: 8, 4, threshold for partial derivatives of the error function as stopping criteria: 0.05

rashomon\_quartet\_train contains just the training data and rashomon\_quartet\_test contains
only the test data.

#### References

P. Biecek, H. Baniecki, M. Krzyziński, D. Cook. Performance is not enough: the story of Rashomon's quartet. Preprint arXiv:2302.13356v2, 2023.

variation\_causal\_quartet

### Gelman Variation Causal Quartet Data

#### Description

This dataset contains 88 observations, each generated under a different mechanism of variation of the treatment effect with respect to some pre-exposure characteristic, z:

- (1) Constant effect
- (2) Low variation
- (3) High variation
- (4) Occasional large effects

#### Usage

variation\_causal\_quartet

# Format

A dataframe with 88 rows and 5 variables:

- dataset: The data generating mechanism
- exposure: exposure
- covariate: a pre-exposure factor
- outcome: outcome
- .causal\_effect: Latent true causal effect

# References

Gelman, A., Hullman, J., & Kennedy, L. (2023). Causal quartets: Different ways to attain the same average treatment effect. arXiv preprint arXiv:2302.12878.

Hullman J (2023). causalQuartet: Create Causal Quartets for Interrogating Average Treatment Effects. R package version 0.0.0.9000.

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