

# Package ‘ImpShrinkage’

January 20, 2025

**Type** Package

**Title** Improved Shrinkage Estimations for Multiple Linear Regression

**Version** 1.0.0

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**Description**

A variety of improved shrinkage estimators in the area of statistical analysis: unrestricted; restricted; preliminary test; improved preliminary test; Stein; and positive-rule Stein. More details can be found in chapter 7 of Saleh, A. K. Md. E. (2006) <ISBN: 978-0-471-56375-4>.

**License** GPL (>= 2)

**URL** <https://github.com/mnrzrad/ImpShrinkage>

**Encoding** UTF-8

**LazyData** false

**RoxygenNote** 7.2.3

**Depends** R (>= 2.10)

**NeedsCompilation** no

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**Repository** CRAN

**Date/Publication** 2023-06-21 19:50:02 UTC

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cement*Hald's Cement Data*

---

**Description**

Heat evolved (cals/gm) in the setting of 13 samples of Portland cement with different percentage weight of chemical components.

**Format**

A data.frame with 13 observations on the following 5 variables.

- x1** percentage weight in clinkers of 3CaO.Al<sub>2</sub>O<sub>3</sub>
- x2** percentage weight in clinkers of 3CaO.SiO<sub>2</sub>
- x3** percentage weight in clinkers of 4CaO.Al<sub>2</sub>O<sub>3</sub>.Fe<sub>2</sub>O<sub>3</sub>
- x4** percentage weight in clinkers of 2CaO.SiO<sub>2</sub>
- y** heat evolved (calories/gram)

**Source**

Woods, H., Steinour, H. H. and Starke, H. R. (1932) Effect of composition of Portland cement on heat evolved during hardening. *Industrial Engineering and Chemistry*, 24, 1207–1214.

**Examples**

```
data("cement")
cement
```

---

```
coefficients.improvedpreliminaryTest
    Extract Model Coefficients
```

---

**Description**

Coefficients extracted from the model object `improvedpreliminaryTest`

**Usage**

```
## S3 method for class 'improvedpreliminaryTest'
coefficients(object, ...)

## S3 method for class 'improvedpreliminaryTest'
coef(object, ...)
```

**Arguments**

`object` An object of class `improvedpreliminaryTest`.  
`...` Other arguments.

**Value**

A vector of coefficients.

**See Also**

`coefficients.unrestricted`, `coefficients.restricted`, `coefficients.preliminaryTest`,  
`coefficients.stein`, `coefficients.positivestein`, `coef.unrestricted`, `coef.restricted`,  
`coef.positivestein`, `coef.stein`, `coef.positivestein`.

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- iptReg(X, y, H, h, alpha = 0.05)
coefficients(model)
coef(model)
```

**coefficients.positivestein**  
*Extract Model Coefficients*

## Description

Coefficients extracted from the model object *positivestein*

## Usage

```
## S3 method for class 'positivestein'
coefficients(object, ...)

## S3 method for class 'positivestein'
coef(object, ...)
```

## Arguments

object	An object of class <i>positivestein</i> .
...	Other arguments.

## Value

A vector of coefficients.

## See Also

[coefficients.unrestricted](#), [coefficients.restricted](#), [coefficients.preliminaryTest](#),  
[coefficients.improvedpreliminaryTest](#), [coefficients.stein](#), [coef.unrestricted](#), [coef.restricted](#),  
[coef.preliminaryTest](#), [coef.improvedpreliminaryTest](#), [coef.stein](#).

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- prstReg(X, y, H, h)
coefficients(model)
coef(model)
```

## coefficients.preliminaryTest

*Extract Model Coefficients*

### Description

Coefficients extracted from the model object `preliminaryTest`

### Usage

```
## S3 method for class 'preliminaryTest'
coefficients(object, ...)

## S3 method for class 'preliminaryTest'
coef(object, ...)
```

### Arguments

<code>object</code>	An object of class <code>preliminaryTest</code> .
...	Other arguments.

### Value

A vector of coefficients.

### See Also

`coefficients.unrestricted`, `coefficients.restricted`, `coefficients.improvedpreliminaryTest`,  
`coefficients.stein`, `coefficients.positivestein`, `coef.unrestricted`, `coef.restricted`,  
`coef.improvedpreliminaryTest`. `coef.stein`, `coef.positivestein`. #'

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- ptReg(X, y, H, h, alpha = 0.05)
coefficients(model)
coef(model)
```

**coefficients.restricted**

*Extract Model Coefficients*

## Description

Coefficients extracted from the model object `restrcited`.

## Usage

```
## S3 method for class 'restricted'
coefficients(object, ...)

## S3 method for class 'restricted'
coef(object, ...)
```

## Arguments

- `object` An object of class `restricted`.
- `...` Other arguments.

## Value

A vector of coefficients.

## See Also

[coefficients.unrestricted](#), [coefficients.preliminaryTest](#), [coefficients.improvedpreliminaryTest](#),  
[coefficients.stein](#), [coefficients.positivestein](#), [coef.unrestricted](#), [coef.preliminaryTest](#),  
[coef.improvedpreliminaryTest](#) [coef.stein](#), [coef.positivestein](#).

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- resReg(X, y, H, h)
coefficients(model)
coef(model)
```

**coefficients.stein**      *Extract Model Coefficients*

## Description

Coefficients extracted from the model object `stein`

## Usage

```
## S3 method for class 'stein'
coefficients(object, ...)

## S3 method for class 'stein'
coef(object, ...)
```

## Arguments

<code>object</code>	An object of class <code>stein</code> .
...	Other arguments.

## Value

A vector of coefficients.

## See Also

[coefficients.unrestricted](#), [coefficients.restricted](#), [coefficients.preliminaryTest](#),  
[coefficients.improvedpreliminaryTest](#), [coefficients.positivestein](#), [coef.unrestricted](#),  
[coef.restricted](#), [coef.preliminaryTest](#), [coef.improvedpreliminaryTest](#), [coef.positivestein](#).

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nr = 3, nc = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- stReg(X, y, H, h)
coefficients(model)
coef(model)
```

**coefficients.unrestricted**

*Extract Model Coefficients*

## Description

Coefficients extracted from the model object `unrestricted`.

## Usage

```
## S3 method for class 'unrestricted'
coefficients(object, ...)

## S3 method for class 'unrestricted'
coef(object, ...)
```

## Arguments

- |                     |  |
|---------------------|--|
| <code>object</code> | An object of class <code>unrestricted</code> . |
| ...                 | Other arguments.                               |

## Value

A vector of coefficients.

## See Also

[coefficients.restricted](#), [coefficients.preliminaryTest](#), [coefficients.improvedpreliminaryTest](#),  
[coefficients.stein](#), [coefficients.positivestein](#), [coef.restricted](#), [coef.preliminaryTest](#),  
[coef.improvedpreliminaryTest](#) [coef.stein](#), [coef.positivestein](#).

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
model <- unrReg(X, y)
coefficients(model)
coef(model)
```

**fitted.improvedpreliminaryTest**  
*Extract Model Fitted Values*

## Description

Fitted values based on object `improvedpreliminaryTest`.

## Usage

```
## S3 method for class 'improvedpreliminaryTest'
fitted(object, ...)
```

## Arguments

object	An object of class <code>improvedpreliminaryTest</code> .
...	Other arguments.

## Value

A vector of fitted values.

## See Also

[fitted.unrestricted](#), [fitted.restricted](#), [fitted.preliminaryTest](#), [fitted.stein](#), [fitted.positivestein](#).

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
```

```
model <- iptReg(X, y, H, h, alpha = 0.05)
fitted(model)
```

**fitted.positivestein** *Extract Model Fitted Values*

## Description

Fitted values based on object `positivestein`.

## Usage

```
## S3 method for class 'positivestein'
fitted(object, ...)
```

## Arguments

- `object` An object of class `positivestein`.
- `...` Other arguments.

## Value

A vector of fitted values.

## See Also

`fitted.unrestricted`, `fitted.restricted`, `fitted.preliminaryTest`, `fitted.improvedpreliminaryTest`, `fitted.stein`.

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- prstReg(X, y, H, h)
fitted(model)
```

---

fitted.preliminaryTest  
Extract Model Fitted Values

---

## Description

Fitted values based on object preliminaryTest.

## Usage

```
## S3 method for class 'preliminaryTest'  
fitted(object, ...)
```

## Arguments

- object        An object of class preliminaryTest.  
...            Other arguments.

## Value

A vector of fitted values.

## See Also

[fitted.unrestricted](#), [fitted.restricted](#), [fitted.improvedpreliminaryTest](#), [fitted.stein](#),  
[fitted.positivestein](#)

## Examples

```
n_obs <- 100  
p_vars <- 5  
beta <- c(2, 1, 3, 0, 5)  
simulated_data <- simdata(n = n_obs, p = p_vars, beta)  
X <- simulated_data$X  
y <- simulated_data$y  
p <- ncol(X)  
# H beta = h  
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)  
h <- rep(0, nrow(H))  
model <- ptReg(X, y, H, h, alpha = 0.05)  
fitted(model)
```

---

**fitted.restricted**      *Extract Model Fitted Values*

---

## Description

Fitted values based on object `restrcited`.

## Usage

```
## S3 method for class 'restricted'
fitted(object, ...)
```

## Arguments

<code>object</code>	An object of class <code>restricted</code> .
<code>...</code>	Other arguments.

## Value

Fitted values extracted from the object `restricted`.

## See Also

[fitted.unrestricted](#), [fitted.preliminaryTest](#), [fitted.improvedpreliminaryTest](#), [fitted.stein](#),  
[fitted.positivestein](#)

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- resReg(X, y, H, h)
fitted(model)
```

---

**fitted.stein**      *Extract Model Fitted Values*

---

**Description**

Fitted values based on object `stein`.

**Usage**

```
## S3 method for class 'stein'  
fitted(object, ...)
```

**Arguments**

object	An object of class <code>stein</code> .
...	Other arguments.

**Value**

A vector of fitted values.

**See Also**

[fitted.unrestricted](#), [fitted.restricted](#), [fitted.preliminaryTest](#), [fitted.improvedpreliminaryTest](#),  
[fitted.positivestein](#)

**Examples**

```
n_obs <- 100  
p_vars <- 5  
beta <- c(2, 1, 3, 0, 5)  
simulated_data <- simdata(n = n_obs, p = p_vars, beta)  
X <- simulated_data$X  
y <- simulated_data$y  
p <- ncol(X)  
# H beta = h  
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nr = 3, nc = p, byrow = TRUE)  
h <- rep(0, nrow(H))  
model <- stReg(X, y, H, h)  
fitted(model)
```

---

**fitted.unrestricted**      *Extract Model Fitted Values*

---

### Description

Fitted values based on object `unrestricted`.

### Usage

```
## S3 method for class 'unrestricted'
fitted(object, ...)
```

### Arguments

<code>object</code>	An object of class <code>unrestricted</code> .
<code>...</code>	Other arguments.

### Value

A vector of fitted values.

### See Also

[fitted.restricted](#), [fitted.preliminaryTest](#), [fitted.improvedpreliminaryTest](#), [fitted.stein](#), [fitted.positivestein](#).

### Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
model <- unrReg(X, y)
fitted(model)
```

---

iptReg*The improved preliminary test estimator*

---

## Description

This function calculates the improved preliminary test estimator. When the error has a normal distribution, this estimator can be calculated by

$$\hat{\beta}^{iPT} = \hat{\beta}^{PT} - d(\hat{\beta}^U - \hat{\beta}^R)\mathcal{L}^{-1}I(\mathcal{L} > F_{q,n-p}(\alpha))$$

and, when the error has a non-normal distribution, by

$$\hat{\beta}^{iPT} = \hat{\beta}^{PT} - d(\hat{\beta}^U - \hat{\beta}^R)\mathcal{L}^{-1}I(\mathcal{L} > \chi_q^2(\alpha))$$

where  $I(A)$  denotes an indicator function and

- $\hat{\beta}^{PT}$  is the preliminary test estimator; See [ptReg](#)
- $\hat{\beta}^U$  is the unrestricted estimator; See [unrReg](#).
- $\hat{\beta}^R$  is the restricted estimator; See [resReg](#).
- $\mathcal{L}$  is the test statistic. See [teststat](#);
- $F_{q,n-p}(\alpha)$  is the upper  $\alpha$  level critical value of  $F$ -distribution with  $(q, n - p)$  degrees of freedom, calculated using [qf](#);
- $\chi_q^2(\alpha)$  is the upper  $\alpha$  level critical value of  $\chi^2$ -distribution with  $q$  degree of freedom, calculated using [qchisq](#);
- $d$  is the shrinkage factor;
- $\alpha$  is the significance level.

## Usage

```
iptReg(X, y, H, h, alpha, d = NULL, is_error_normal = FALSE)
```

## Arguments

X	Matrix with input observations, of dimension $n \times p$ ; each row is an observation vector.
y	Vector with response observations of size $n$ .
H	A given $q \times p$ matrix.
h	A given $q \times 1$ vector.
alpha	A given significance level.
d	(optional) If not provided (or set to NULL), it will be calculated using $\frac{(q-2) \cdot (n-p)}{q \cdot (n-p+2)}$ .
is_error_normal	logical value indicating whether the errors follow a normal distribution. If <code>is_error_normal</code> is TRUE, the distribution of the test statistics for the null hypothesis is F distribution ( <a href="#">FDist</a> ). On the other hand, if the errors have a non-normal distribution, the asymptotic distribution of the test statistics is $\chi^2$ distribution ( <a href="#">Chisquare</a> ). By default, <code>is_error_normal</code> is set to FALSE.

## Details

The corresponding estimator of  $\sigma^2$  is

$$s^2 = \frac{1}{n-p} (y - X\hat{\beta}^{iPT})^\top (y - X\hat{\beta}^{iPT}).$$

## Value

An object of class `improvedpreliminaryTest` is a list containing at least the following components:

- `coef` A named vector of coefficients.
- `residuals` The residuals, that is, the response values minus fitted values.
- `s2` The estimated variance.
- `fitted.values` The fitted values.

## References

- Saleh, A. K. Md. Ehsanes. (2006). *Theory of Preliminary Test and Stein-Type Estimation With Applications*, Wiley.
- Kaciranlar, S., Akdeniz, S. S. F., Styan, G. P. & Werner, H. J. (1999). A new biased estimators in linear regression and detailed analysis of the widely-analysed dataset on portland cement. *Sankhya, Series B*, 61(3), 443-459.
- Kibria, B. M. Golam (2005). Applications of Some Improved Estimators in Linear Regression, *Journal of Modern Applied Statistical Methods*, 5(2), 367- 380.

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
iptReg(X, y, H, h, alpha = 0.05)

# H beta != h
p <- ncol(X)
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(1, nrow(H))
iptReg(X, y, H, h, alpha = 0.05)

data(cement)
X <- as.matrix(cbind(1, cement[, 1:4]))
y <- cement$y
# Based on Kaciranlar et al. (1999)
```

```

H <- matrix(c(0, 1, -1, 1, 0), nrow = 1, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
iptReg(X, y, H, h, alpha = 0.05)
# Based on Kibria (2005)
H <- matrix(c(0, 1, -1, 1, 0, 0, 0, 1, -1, -1, 0, 1, -1, 0, -1), nrow = 3, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
iptReg(X, y, H, h, alpha = 0.05)

```

**predict.improvedpreliminaryTest**  
*Extract Model Predictions Values*

### Description

Predicted values based on object `improvedpreliminaryTest`.

### Usage

```
## S3 method for class 'improvedpreliminaryTest'
predict(object, newdata, ...)
```

### Arguments

- |         |  |
|---------|--|
| object  | An object of class "improvedpreliminaryTest".  |
| newdata | An optional data frame in which to look for variables with which to predict. If omitted, the fitted values are used. |
| ...     | Other arguments.   |

### Value

A vector of predictions.

### See Also

[predict.unrestricted](#), [predict.restricted](#), [predict.preliminaryTest](#), [predict.stein](#), [predict.positivestein](#).

### Examples

```

n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- iptReg(X, y, H, h, alpha = 0.05)

```

```
predict(model, X)
```

**predict.positivestein** *Extract Model Predictions Values*

## Description

Predicted values based on object `positivestein`.

## Usage

```
## S3 method for class 'positivestein'
predict(object, newdata, ...)
```

## Arguments

- `object` An object of class "positivestein".
- `newdata` An optional data frame in which to look for variables with which to predict. If omitted, the fitted values are used.
- `...` Other arguments.

## Value

A vector of predictions.

## See Also

[predict.unrestricted](#), [predict.restricted](#), [predict.preliminaryTest](#), [predict.improvedpreliminaryTest](#), [predict.stein](#).

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- prstReg(X, y, H, h)
predict(model, X)
```

---

**predict.preliminaryTest**  
*Extract Model Predictions Values*

---

**Description**

Predicted values based on object `preliminaryTest`.

**Usage**

```
## S3 method for class 'preliminaryTest'  
predict(object, newdata, ...)
```

**Arguments**

- `object` An object of class "preliminaryTest".  
`newdata` An optional data frame in which to look for variables with which to predict. If omitted, the fitted values are used.  
`...` Other arguments.

**Value**

A vector of predictions.

**See Also**

[predict.unrestricted](#), [predict.restricted](#), [predict.improvedpreliminaryTest](#), [predict.stein](#), [predict.positivestein](#).

**Examples**

```
n_obs <- 100  
p_vars <- 5  
beta <- c(2, 1, 3, 0, 5)  
simulated_data <- simdata(n = n_obs, p = p_vars, beta)  
X <- simulated_data$X  
y <- simulated_data$y  
p <- ncol(X)  
# H beta = h  
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)  
h <- rep(0, nrow(H))  
model <- ptReg(X, y, H, h, alpha = 0.05)  
predict(model, X)
```

**predict.restricted**      *Extract Model Predictions Values*

## Description

Predicted values based on object restricted.

## Usage

```
## S3 method for class 'restricted'
predict(object, newdata, ...)
```

## Arguments

- |         |  |
|---------|--|
| object  | An object of class <b>restricted</b> .   |
| newdata | An optional data frame in which to look for variables with which to predict. If omitted, the fitted values are used. |
| ...     | Other arguments.   |

## Value

A vector of predictions.

## See Also

[predict.unrestricted](#), [predict.preliminaryTest](#), [predict.improvedpreliminaryTest](#), [predict.stein](#), [predict.positivestein](#).

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- resReg(X, y, H, h)
predict(model, X)
```

---

<code>predict.stein</code>	<i>Extract Model Predictions Values</i>
----------------------------	---

---

## Description

Predicted values based on object `stein`.

## Usage

```
## S3 method for class 'stein'
predict(object, newdata, ...)
```

## Arguments

- `object` An object of class "stein".
- `newdata` An optional data frame in which to look for variables with which to predict. If omitted, the fitted values are used.
- `...` Other arguments.

## Value

A vector of predictions.

## See Also

[predict.unrestricted](#), [predict.restricted](#), [predict.preliminaryTest](#), [predict.improvedpreliminaryTest](#), [predict.positivestein](#).

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nr = 3, nc = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- stReg(X, y, H, h)
predict(model, X)
```

**predict.unrestricted    Extract Model Predictions Values**

---

## Description

Predicted values based on object `unrestricted`.

## Usage

```
## S3 method for class 'unrestricted'
predict(object, newdata, ...)
```

## Arguments

- |                      |  |
|----------------------|--|
| <code>object</code>  | An object of class <code>unrestricted</code> .   |
| <code>newdata</code> | An optional data frame in which to look for variables with which to predict. If omitted, the fitted values are used. |
| <code>...</code>     | Other arguments.   |

## Value

A vector of predictions.

## See Also

[predict.restricted](#), [predict.preliminaryTest](#), [predict.improvedpreliminaryTest](#), [predict.stein](#), [predict.positivestein](#).

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
model <- unrReg(X, y)
predict(model, X)
```

---

prstReg*The positive-rule Stein estimator*

---

**Description**

This function calculates the positive-rule Stein estimator. This estimator is an improved version of the Stein estimator, where only the positive part of the shrinking factor is considered. It may be calculated by

$$\hat{\beta}^{S+} = \hat{\beta}^S + (1 + d\mathcal{L}^{-1})I(\mathcal{L} > d)(\hat{\beta}^U - \hat{\beta}^R)$$

where  $I(A)$  denotes an indicator function and

- $\hat{\beta}^S$  is the Stein estimator; See [stReg](#).
- $\hat{\beta}^U$  is the unrestricted estimator; See [unrReg](#).
- $\hat{\beta}^R$  is the restricted estimator; See [resReg](#).
- $\mathcal{L}$  is the test statistic. See [teststat](#);
- $d$  is the shrinkage factor.

**Usage**

```
prstReg(X, y, H, h, d = NULL, is_error_normal = FALSE)
```

**Arguments**

X	Matrix with input observations, of dimension n x p; each row is an observation vector.
y	Vector with response observations of size n.
H	A given q x p matrix.
h	A given q x 1 vector.
d	(optional) If not provided (or set to NULL), it will be calculated using $\frac{(q-2)\cdot(n-p)}{q\cdot(n-p+2)}$ .
is_error_normal	logical value indicating whether the errors follow a normal distribution. If is_error_normal is TRUE, the distribution of the test statistics for the null hypothesis is F distribution ( <a href="#">FDist</a> ). On the other hand, if the errors have a non-normal distribution, the asymptotic distribution of the test statistics is $\chi^2$ distribution ( <a href="#">Chisquare</a> ). By default, is_error_normal is set to FALSE.

**Details**

The corresponding estimator of  $\sigma^2$  is given by

$$s^2 = \frac{1}{n-p}(y - X\hat{\beta}^{S+})^\top(y - X\hat{\beta}^{S+}).$$

### Value

An object of class `pst` is a list containing at least the following components:

- `coef` A named vector of coefficients.
- `residuals` The residuals, that is, the response values minus fitted values.
- `s2` The estimated variance.
- `fitted.values` The fitted values.

### References

- Saleh, A. K. Md. Ehsanes. (2006). *Theory of Preliminary Test and Stein-Type Estimation With Applications*, Wiley.
- Kaciranlar, S., Akdeniz, S. S. F., Styan, G. P. & Werner, H. J. (1999). A new biased estimators in linear regression and detailed analysis of the widely-analysed dataset on portland cement. *Sankhya, Series B*, 61(3), 443-459.
- Kibria, B. M. Golam (2005). Applications of Some Improved Estimators in Linear Regression, *Journal of Modern Applied Statistical Methods*, 5(2), 367- 380.

### Examples

```

n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nr = 3, nc = p, byrow = TRUE)
h <- rep(0, nrow(H))
prstReg(X, y, H, h)

# H beta != h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nr = 3, nc = p, byrow = TRUE)
h <- rep(1, nrow(H))
prstReg(X, y, H, h)

data(cement)
X <- as.matrix(cbind(1, cement[, 1:4]))
y <- cement$y
# Based on Kaciranlar et al. (1999)
H <- matrix(c(0, 1, -1, 1, 0), nrow = 1, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
prstReg(X, y, H, h)
# Based on Kibria (2005)
H <- matrix(c(0, 1, -1, 1, 0, 0, 0, 1, -1, -1, 0, 1, -1, 0, -1), nrow = 3, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
prstReg(X, y, H, h)

```

## Description

This function calculates the preliminary test. When the error has a normal distribution, the test statistic is given by

$$\hat{\beta}^{PT} = \hat{\beta}^U - (\hat{\beta}^U - \hat{\beta}^R)I(\mathcal{L} \leq F_{q,n-p}(\alpha))$$

and, if the error has a non-normal distribution, is given by

$$\hat{\beta}^{PT} = \hat{\beta}^U - (\hat{\beta}^U - \hat{\beta}^R)I(\mathcal{L} \leq \chi_q^2(\alpha))$$

where  $I(A)$  denotes an indicator function and

- $\hat{\beta}^U$  is the unrestricted estimator; See [unrReg](#).
- $\hat{\beta}^R$  is the restricted estimator; See [resReg](#).
- $\mathcal{L}$  is the test statistic. See [teststat](#);
- $F_{q,n-p}(\alpha)$  is the upper  $\alpha$  level critical value of  $F$ -distribution with  $(q, n - p)$  degrees of freedom, calculated using [qf](#);
- $\chi_q^2(\alpha)$  is the upper  $\alpha$  level critical value of  $\chi^2$ -distribution with  $q$  degree of freedom, calculated using [qchisq](#);
- $\alpha$ : the significance level.

## Usage

```
ptReg(X, y, H, h, alpha, is_error_normal = FALSE)
```

## Arguments

X	Matrix with input observations, of dimension $n \times p$ ; each row is an observation vector.
y	Vector with response observations of size $n$ .
H	A given $q \times p$ matrix.
h	A given $q \times 1$ vector.
alpha	A given significance level.
is_error_normal	logical value indicating whether the errors follow a normal distribution. If <code>is_error_normal</code> is TRUE, the distribution of the test statistics for the null hypothesis is F distribution ( <a href="#">FDist</a> ). On the other hand, if the errors have a non-normal distribution, the asymptotic distribution of the test statistics is $\chi^2$ distribution ( <a href="#">Chisquare</a> ). By default, <code>is_error_normal</code> is set to FALSE.

## Details

The corresponding estimator of  $\sigma^2$  is

$$s^2 = \frac{1}{n-p} (y - X\hat{\beta}^{PT})^\top (y - X\hat{\beta}^{PT}).$$

## Value

An object of class `preliminaryTest` is a list containing at least the following components:

- `coef` A named vector of coefficients.
- `residuals` The residuals, that is, the response values minus fitted values.
- `s2` The estimated variance.
- `fitted.values` The fitted values.

## References

- Saleh, A. K. Md. Ehsanes. (2006). *Theory of Preliminary Test and Stein-Type Estimation With Applications*, Wiley.
- Kaciranlar, S., Akdeniz, S. S. F., Styan, G. P. & Werner, H. J. (1999). A new biased estimators in linear regression and detailed analysis of the widely-analysed dataset on portland cement. *Sankhya, Series B*, 61(3), 443-459.
- Kibria, B. M. Golam (2005). Applications of Some Improved Estimators in Linear Regression, *Journal of Modern Applied Statistical Methods*, 5(2), 367- 380.

## Examples

```

n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
ptReg(X, y, H, h, alpha = 0.05)

# H beta != h
p <- ncol(X)
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(1, nrow(H))
ptReg(X, y, H, h, alpha = 0.05)

data(cement)
X <- as.matrix(cbind(1, cement[, 1:4]))
y <- cement$y
# Based on Kaciranlar et al. (1999)
H <- matrix(c(0, 1, -1, 1, 0), nrow = 1, ncol = 5, byrow = TRUE)

```

```

h <- rep(0, nrow(H))
ptReg(X, y, H, h, alpha = 0.05)
# Based on Kibria (2005)
H <- matrix(c(0, 1, -1, 1, 0, 0, 1, -1, -1, 0, 1, -1, 0, -1), nrow = 3, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
ptReg(X, y, H, h, alpha = 0.05)

```

**residuals.improvedpreliminaryTest**  
*Extract Model Residuals*

### Description

Residuals values based on model object `improvedpreliminaryTest`.

### Usage

```
## S3 method for class 'improvedpreliminaryTest'
residuals(object, ...)
```

### Arguments

- |        |   |
|--------|---|
| object | An object of class <code>improvedpreliminaryTest</code> . |
| ...    | Other arguments.  |

### Value

A vector of residuals.

### See Also

`residuals.unrestricted`, `residuals.restricted`, `residuals.preliminaryTest`, `residuals.stein`,  
`residuals.positivestein`,

### Examples

```

n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- iptReg(X, y, H, h, alpha = 0.05)
residuals(model)

```

---

**residuals.positivestein**  
*Extract Model Residuals*

---

## Description

Residuals values based on model object *positivestein*.

## Usage

```
## S3 method for class 'positivestein'
residuals(object, ...)
```

## Arguments

- |        |   |
|--------|---|
| object | An object of class <i>positivestein</i> . |
| ...    | Other arguments.                          |

## Value

A vector of residuals.

## See Also

[residuals.unrestricted](#), [residuals.restricted](#), [residuals.preliminaryTest](#), [residuals.improvedpreliminary](#),  
[residuals.stein](#).

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- prstReg(X, y, H, h)
residuals(model)
```

---

residuals.preliminaryTest  
Extract Model Residuals

---

**Description**

Residuals values based on model object preliminaryTest.

**Usage**

```
## S3 method for class 'preliminaryTest'  
residuals(object, ...)
```

**Arguments**

object            An object of class preliminaryTest.  
...                Other arguments.

**Value**

A vector of residuals.

**See Also**

[residuals.unrestricted](#), [residuals.restricted](#), [residuals.improvedpreliminaryTest](#), [residuals.stein](#),  
[residuals.positivestein](#).

**Examples**

```
n_obs <- 100  
p_vars <- 5  
beta <- c(2, 1, 3, 0, 5)  
simulated_data <- simdata(n = n_obs, p = p_vars, beta)  
X <- simulated_data$X  
y <- simulated_data$y  
p <- ncol(X)  
# H beta = h  
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)  
h <- rep(0, nrow(H))  
model <- ptReg(X, y, H, h, alpha = 0.05)  
residuals(model)
```

`residuals.restricted` *Extract Model Residuals*

## Description

Residuals values based on model object `restricted`.

## Usage

```
## S3 method for class 'restricted'
residuals(object, ...)
```

## Arguments

<code>object</code>	An object of class <code>restricted</code> .
<code>...</code>	Other arguments.

## Value

A vector of residuals.

`residuals.unrestricted`, `residuals.preliminaryTest`, `residuals.improvedpreliminaryTest`,  
`residuals.stein`, `residuals.positivestein`.

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- resReg(X, y, H, h)
residuals(model)
```

`residuals.stein` *Extract Model Residuals*

## Description

Residuals values based on model object `stein`.

**Usage**

```
## S3 method for class 'stein'
residuals(object, ...)
```

**Arguments**

object	An object of class <code>stein</code> .
...	Other arguments.

**Value**

A vector of residuals.

**See Also**

`residuals.unrestricted`, `residuals.restricted`, `residuals.preliminaryTest`, `residuals.improvedpreliminary`,  
`residuals.positivestein`,

**Examples**

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nr = 3, nc = p, byrow = TRUE)
h <- rep(0, nrow(H))
model <- stReg(X, y, H, h)
residuals(model)
```

**residuals.unrestricted**

*Extract Model Residuals*

**Description**

Residuals values based on model object `unrestricted`.

**Usage**

```
## S3 method for class 'unrestricted'
residuals(object, ...)
```

**Arguments**

- `object` An object of class `unrestricted`.  
`...` Other arguments.

**Value**

A vector of residuals.

**See Also**

`residuals.restricted`, `residuals.preliminaryTest`, `residuals.improvedpreliminaryTest`  
`residuals.stein`, `residuals.positivestein`.

**Examples**

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
model <- unrReg(X, y)
residuals(model)
```

`resReg` *The restricted estimator*

**Description**

This function calculates the restricted estimator using

$$\hat{\beta}^R = \hat{\beta}^U - (X^\top X)^{-1} H^\top (H(X^\top X)^{-1} H^\top)^{-1} (H\hat{\beta}^U - h)$$

where

- $\hat{\beta}^U$  is the unrestricted estimator; See `unrReg`.
- $H\beta = h$  represents a subspace of the parameter space induced by the non-sample information. Here,  $H$  is a known  $q \times p$  matrix, and  $h$  is a known  $q$ -vector.

**Usage**

`resReg(X, y, H, h)`

**Arguments**

- `X` Matrix with input observations, of dimension  $n \times p$ ; each row is an observation vector.  
`y` Vector with response observations of size  $n$ .  
`H` A given  $q \times p$  matrix.  
`h` A given  $q \times 1$  vector.

## Details

#' The corresponding estimator of  $\sigma^2$  is

$$s^2 = \frac{1}{n-p}(y - X\hat{\beta}^R)^\top(y - X\hat{\beta}^R).$$

## Value

An object of class `restricted` is a list containing at least the following components:

`coef` A named vector of coefficients.

`residuals` The residuals, that is, the response values minus fitted values.

`s2` The estimated variance.

`fitted.values` The fitted values.

## References

Saleh, A. K. Md. Ehsanes. (2006). *Theory of Preliminary Test and Stein-Type Estimation With Applications*, Wiley.

Kaciranlar, S., Akdeniz, S. S. F., Styan, G. P. & Werner, H. J. (1999). A new biased estimators in linear regression and detailed analysis of the widely-analysed dataset on portland cement. *Sankhya, Series B*, 61(3), 443-459.

Kibria, B. M. Golam (2005). Applications of Some Improved Estimators in Linear Regression, *Journal of Modern Applied Statistical Methods*, 5(2), 367- 380.

## Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
resReg(X, y, H, h)

# H beta != h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(1, nrow(H))
resReg(X, y, H, h)

data(cement)
X <- as.matrix(cbind(1, cement[, 1:4]))
y <- cement$y
# Based on Kaciranlar et al. (1999)
H <- matrix(c(0, 1, -1, 1, 0), nrow = 1, ncol = 5, byrow = TRUE)
```

```

h <- rep(0, nrow(H))
resReg(X, y, H, h)
# Based on Kibria (2005)
H <- matrix(c(0, 1, -1, 1, 0, 0, 1, -1, -1, 0, 1, -1, 0, -1), nrow = 3, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
resReg(X, y, H, h)

```

**simdata***Simulation data***Description**

This function generates a toy example. The error term,  $\varepsilon$ , and the design matrix,  $X$ , are simulated from standard normal distributions,  $\mathcal{N}(0, 1)$ , using the `rnorm` function. Given the true parameter vector,  $\beta$ , the response vector,  $y$ , is calculated as

$$y = X\beta + \varepsilon.$$

**Usage**

```
simdata(n, p, beta, seed = NULL)
```

**Arguments**

<code>n</code>	Number of observations.
<code>p</code>	Number of variables.
<code>beta</code>	Regression parameter.
<code>seed</code>	(Optional) The random seed for reproducibility. Default is <code>NULL</code> .

**Value**

A list containing the following components:

`X` a matrix of dimensions  $n \times p$ .

`y` a numeric vector of length  $n$ .

**References**

Saleh, A. K. Md. Ehsanes. (2006). *Theory of Preliminary Test and Stein-Type Estimation With Applications*, Wiley.

**Examples**

```

simulated_data <- simdata(n = 100, p = 5, beta = c(2, 1, 3, 0, 5))
X <- simulated_data$X
y <- simulated_data$y
X
y

```

## Description

This function can be used to calculate the Stein estimator using

$$\hat{\beta}^S = \hat{\beta}^U - d\mathcal{L}^{-1}(\hat{\beta}^U - \hat{\beta}^R)$$

where

- $\hat{\beta}^U$  is the unrestricted estimator; See [unrReg](#).
- $\hat{\beta}^R$  is the restricted estimator; See [resReg](#).
- $\mathcal{L}$  is the test statistic. See [teststat](#);
- $d$  is the shrinkage factor.

## Usage

```
stReg(X, y, H, h, d = NULL, is_error_normal = FALSE)
```

## Arguments

X	Matrix with input observations, of dimension n x p; each row is an observation vector.
y	Vector with response observations of size n.
H	A given q x p matrix.
h	A given q x 1 vector.
d	(Optional) If not provided (or set to NULL), it will be set to be equal to $\frac{(q-2)\cdot(n-p)}{q\cdot(n-p+2)}$ .
is_error_normal	logical value indicating whether the errors follow a normal distribution. If is_error_normal is TRUE, the distribution of the test statistics for the null hypothesis is <a href="#">FDist</a> . On the other hand, if the errors have a non-normal distribution, the asymptotic distribution of the test statistics is <a href="#">Chisquare</a> . By default, is_error_normal is set to FALSE.

## Details

The corresponding estimator of  $\sigma^2$  is

$$s^2 = \frac{1}{n-p}(y - X\hat{\beta}^S)^\top(y - X\hat{\beta}^S).$$

### Value

An object of class `stein` is a list containing at least the following components:

`coef` A vector of coefficients.

`residuals` The residuals, that is, the response values minus the fitted values.

`s2` The estimated variance.

`fitted.values` The fitted values.

### References

Saleh, A. K. Md. Ehsanes. (2006). *Theory of Preliminary Test and Stein-Type Estimation With Applications*, Wiley.

Kaciranlar, S., Akdeniz, S. S. F., Styan, G. P. & Werner, H. J. (1999). A new biased estimators in linear regression and detailed analysis of the widely-analysed dataset on portland cement. *Sankhya, Series B*, 61(3), 443-459.

Kibria, B. M. Golam (2005). Applications of Some Improved Estimators in Linear Regression, *Journal of Modern Applied Statistical Methods*, 5(2), 367- 380.

### Examples

```
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
stReg(X, y, H, h)

# H beta != h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(1, nrow(H))
stReg(X, y, H, h)

data(cement)
X <- as.matrix(cbind(1, cement[, 1:4]))
y <- cement$y
# Based on Kaciranlar et al. (1999)
H <- matrix(c(0, 1, -1, 1, 0), nrow = 1, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
stReg(X, y, H, h)
# Based on Kibria (2005)
H <- matrix(c(0, 1, -1, 1, 0, 0, 1, -1, -1, 0, 1, -1, 0, -1), nrow = 3, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
stReg(X, y, H, h)
```

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teststat	<i>Test-Statistics</i>
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## Description

This function calculates the test statistics, assuming  $\mathcal{H}_0 : H\beta = h$ . When the error has a normal distribution, it is defined as

$$\mathcal{L} = \frac{(H\hat{\beta}^U - h)^\top (H(X^\top X)^{-1}H^\top)^{-1}(H\hat{\beta}^U - h)}{qs_{unr}^2}$$

and when the error has a non-normal distribution, as

$$\mathcal{L} = \frac{(H\hat{\beta}^U - h)^\top (H(X^\top X)^{-1}H^\top)^{-1}(H\hat{\beta}^U - h)}{s_{unr}^2}$$

where

- $\hat{\beta}^U$  is the unrestricted estimator; See [unrReg](#).
- $q$  is the number of restrictions, i.e., the number of rows of known matrix  $H$ ;
- $s_{unr}^2$  is the corresponding unrestricted estimator of  $\sigma^2$ .

## Usage

```
teststat(X, y, H, h, is_error_normal = FALSE)
```

## Arguments

X            Matrix with input observations, of dimension n x p; each row is an observation vector.

y            Vector with response observations of size n.

H            A given q x p matrix.

h            A given q x 1 vector.

is\_error\_normal

logical value indicating whether the errors follow a normal distribution. If `is_error_normal` is TRUE, the distribution of the test statistics for the null hypothesis is the F distribution ([FDist](#)). On the other hand, if the errors have a non-normal distribution, the asymptotic distribution of the test statistics is the  $\chi^2$  distribution ([Chisquare](#)). By default, `is_error_normal` is set to FALSE.

## Value

The value of the test statistic.

## References

- Saleh, A. K. Md. Ehsanes. (2006). *Theory of Preliminary Test and Stein-Type Estimation With Applications*, Wiley.
- Kaciranlar, S., Akdeniz, S. S. F., Styan, G. P. & Werner, H. J. (1999). A new biased estimators in linear regression and detailed analysis of the widely-analysed dataset on portland cement. *Sankhya, Series B*, 61(3), 443-459.
- Kibria, B. M. Golam (2005). Applications of Some Improved Estimators in Linear Regression, *Journal of Modern Applied Statistical Methods*, 5(2), 367- 380.

## Examples

```

n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p_vars, beta)
X <- simulated_data$x
y <- simulated_data$y
p <- ncol(X)
# H beta = h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(0, nrow(H))
teststat(X, y, H, h)

# H beta != h
H <- matrix(c(1, 1, -1, 0, 0, 1, 0, 1, 0, -1, 0, 0, 0, 1, 0), nrow = 3, ncol = p, byrow = TRUE)
h <- rep(1, nrow(H))
teststat(X, y, H, h)

data(cement)
X <- as.matrix(cbind(1, cement[, 1:4]))
y <- cement$y
# Based on Kaciranlar et al. (1999)
H <- matrix(c(0, 1, -1, 1, 0), nrow = 1, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
teststat(X, y, H, h)
# Based on Kibria (2005)
H <- matrix(c(0, 1, -1, 1, 0, 0, 0, 1, -1, -1, 0, 1, -1, 0, -1), nrow = 3, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
teststat(X, y, H, h)

```

## Description

This function calculates the unrestricted estimator as

$$\hat{\beta}^U = (X^\top X)^{-1} X^\top y$$

where  $\top$  denotes the transpose of a matrix. It is important to note that the input matrices  $X$  and  $y$  should be standardized, for example, by using `scale`. Alternatively, the user can employ `lm` to obtain this estimator, but it is crucial to remember to set `intercept = FALSE`.

## Usage

```
unrReg(X, y)
```

## Arguments

- |                |  |
|----------------|--|
| <code>X</code> | Matrix with input observations, of dimension $n \times p$ , where each row is an observation vector; |
| <code>y</code> | Vector with response observations of size $n$ .  |

## Details

The corresponding unrestricted estimator of  $\sigma^2$  is

$$s^2 = \frac{1}{n-p} (y - X\hat{\beta}^U)^\top (y - X\hat{\beta}^U).$$

## Value

An object of class `unrestricted` is a list containing at least the following components:

- `coef` A named vector of coefficients.
- `residuals` The residuals, that is, the response values minus fitted values.
- `s2` The estimated variance.
- `fitted.values` The fitted values.

## References

Saleh, A. K. Md. Ehsanes. (2006). *Theory of Preliminary Test and Stein-Type Estimation With Applications*, Wiley.

## Examples

```
data(cement)
n_obs <- 100
p_vars <- 5
beta <- c(2, 1, 3, 0, 5)
simulated_data <- simdata(n = n_obs, p = p_vars, beta)
X <- simulated_data$X
y <- simulated_data$y
unrReg(X, y)

data(cement)
X <- as.matrix(cbind(1, cement[, 1:4]))
y <- cement$y
# Based on Kaciranlar et al. (1999)
H <- matrix(c(0, 1, -1, 1, 0), nrow = 1, ncol = 5, byrow = TRUE)
```

```
h <- rep(0, nrow(H))
unrReg(X, y)

H <- matrix(c(0, 1, -1, 1, 0, 0, 0, 1, -1, -1, 0, 1, -1, 0, -1), nrow = 3, ncol = 5, byrow = TRUE)
h <- rep(0, nrow(H))
unrReg(X, y)
```

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